Hyperspectral optical tomography of intrinsic signals in the rat cortex

Soren D. Konecky
Robert H. Wilson
Nathan Hagen
Amaan Mazhar
Tomasz S. Tkaczyk
Ron D. Frostig
Bruce J. Tromberg
Hyperspectral optical tomography of intrinsic signals in the rat cortex

Soren D. Konecky, a Robert H. Wilson, a Nathan Hagen, b Amaan Mazhar, a,d Tomasz S. Tkaczyk, b Ron D. Frostig, c,d and Bruce J. Tromberg a,d,*

aUniversity of California, Irvine, Beckman Laser Institute and Medical Clinic, Laser Microbeam and Medical Program, 1002 Health Sciences Road, Irvine, California 92612, United States
bRice University, Department of Biomedical Engineering, 6500 Main Street, Houston, Texas 77030, United States
cUniversity of California, Irvine, Department of Neurobiology and Behavior, 2205 McGaugh Hall, Irvine, California 92697, United States
dUniversity of California, Irvine, Department of Biomedical Engineering, 5200 Engineering Hall, Irvine, California 92697, United States

Abstract. We introduce a tomographic approach for three-dimensional imaging of evoked hemodynamic activity, using broadband illumination and diffuse optical tomography (DOT) image reconstruction. Changes in diffuse reflectance in the rat somatosensory cortex due to stimulation of a single whisker were imaged at a frame rate of 5 Hz using a hyperspectral image mapping spectrometer. In each frame, images in 38 wavelength bands from 484 to 652 nm were acquired simultaneously. For data analysis, we developed a hyperspectral DOT algorithm that used the Rytov approximation to quantify changes in tissue concentration of oxyhemoglobin (ctHbO2) and deoxyhemoglobin (ctHb) in three dimensions. Using this algorithm, the maximum changes in ctHbO2 and ctHb were found to occur at 0.29 ± 0.02 and 0.66 ± 0.04 mm beneath the surface of the cortex, respectively. Rytov tomographic reconstructions revealed maximal spatially localized increases and decreases in ctHbO2 and ctHb of 321 ± 53 and 555 ± 96 nM, respectively, with these maximum changes occurring at 4 ± 0.2 s poststimulus. The localized optical signals from the Rytov approximation were greater than those from modified Beer–Lambert, likely due in part to the inability of planar reflectance to account for partial volume effects. © 2015 SPIE

Keywords: optical brain imaging; hyperspectral imaging; optical tomography; hemodynamic imaging; neurovascular coupling; wide-field optical imaging.

Paper 15021R received Apr. 29, 2015; accepted for publication Oct. 19, 2015; published online Nov. 12, 2015.

1 Introduction

The study of cerebral hemodynamics is important for treating brain pathologies, neuroimaging, and fundamental neuroscience. Cerebral hemodynamics plays a critical role not only in cerebrovascular diseases such as stroke but also in neurodegenerative diseases such as Alzheimer’s disease and age-related neurodegeneration. Hemodynamic activity is also the basis for functional magnetic resonance imaging (fMRI), which does not measure neuronal activity directly but instead measures the hemodynamic response that accompanies neuronal activity. Hemodynamic activity may play a direct role in information processing itself, in addition to its supportive role of delivering glucose and oxygen. Thus, the ability to quantitatively measure cerebral hemodynamics with high temporal and spatial resolution is important for fundamental neuroscience research and for developing new treatments and therapeutic targets for brain pathologies.

Intrinsic signal optical imaging (ISOI) is a powerful tool for imaging the hemodynamic responses to evoked activity of the brain in animal models. ISOI is a camera-based technique that relies on the fact that hemodynamic activity changes the light intensity remitted from an illuminated brain. It allows for high spatial (~10 μm) and temporal (<0.1 s) resolution over a wide field of view. It is low cost, noninvasive, and can be used in chronic imaging studies in animal models. However, despite its widespread use, ISOI only provides two-dimensional (2-D) planar images, and thus cannot localize the depth in the cortex at which hemodynamic changes occur.

The need for three-dimensional (3-D) determination of hemoglobin concentration and oxygenation state has been a major factor driving the growth of the field of diffuse optical tomography (DOT). Researchers have used the temporal profile of pulsed sources and large arrays of fibers to localize the depth of hemodynamic activity in humans. Optical tomography of cerebral hemodynamics of small animals has also been performed using optical fibers and fast scanning. However, fiber-based approaches tend to be constrained by the number of discrete (fiber optic) source and detector probes that are used, and by the vast dynamic range required for different source–detector separations.

For small-animal imaging experiments in which only the first ~1 – 2 mm of tissue needs to be probed, hyperspectral camera-based imaging may provide a simple approach to acquire depth-resolved images with high spatial and temporal resolution. This would provide ISOI with the ability to determine whether optical signals originate from vasculature in the parenchyma or at the surface of the cortex. Quantifying these signals would provide a more complete picture of the spatiotemporal features of the hemodynamic response and may help to determine the signaling mechanisms underlying the coupling between neuronal and vascular activity. While several studies have used confocal and multiphoton microscopy to look at the flow of...
red blood cells, the dilation of individual vessels, and the distribution of oxygen tension, these approaches are based on exogenous probes and are generally only viable for depths up to \( \sim 500 \) \( \mu \)m. In addition, microscopy-based methods necessarily probe a limited number of microvascular structures in a small field of view.

Many researchers have performed ISOI at multiple wavelengths and used the differing spectral features of oxy- and deoxyhemoglobin to produce 2-D maps of changes in oxy- and deoxyhemoglobin concentration. Practical constraints typically limit the ability of serial spectral scanning to simultaneously provide both spatial and spectroscopic information. Spectroscopic approaches generally sacrifice imaging performance by either collecting data at a single point or diffusing light passing through a slit in order to obtain a one-dimensional (1-D) “image.” Other methods have used a filter wheel or flashing LEDs to serially obtain images at multiple wavelengths. While effective, these methods are limited by the trade-off between the number of wavelengths measured and temporal resolution. Recent attempts to overcome these limitations include approaches using a combination of beam splitters and filters to image at four wavelengths simultaneously and methods using concurrent CCD-based imaging and fiber-based spectroscopy in a single experiment. Ideally, one would like to acquire high-resolution images that contain full spectral information at every location on the cortex, and use this data to reconstruct 3-D maps of the changes in tissue hemodynamics.

In this paper, we describe image mapping spectroscopy (IMS) to image intrinsic optical signals following sensory stimulation in the rat. IMS is a new method for hyperspectral imaging capable of forming planar 2-D images in multiple distinct wavelength bins. In this work, we employed an IMS camera operating at 5 Hz to image with 38 spectral bands from 484 to 652 nm in a single snapshot. Unlike other hyperspectral imaging methods, IMS has high optical throughput and does not require scanning or image reconstruction to produce a set of spectrally binned images. As a result, IMS can acquire hyperspectral images at the frame rate of the camera. Thus, IMS is ideal for high-resolution hyperspectral imaging of the small and transient changes in light intensity following sensory stimulation.

To take advantage of the IMS spectral content, we developed a hyperspectral optical tomography algorithm to generate 3-D images of poststimulus changes in oxy- and deoxyhemoglobin concentrations from the acquired reflectance data. Multiwavelength depth localization has recently been studied by several groups for subsurface fluorescence imaging, in which distortions in the emission profiles resulting from the absorption of the emitted light as it travels to the surface are used to estimate the depth of the fluorescent object. Our tomographic reconstruction algorithm, based on the Rytov approximation, takes advantage of the distortion of the reflectance spectra to localize the depth at which the concentrations of tissue absorbers (i.e., oxy- and deoxyhemoglobin) change. Previous studies have employed the Rytov approximation for tomographic reconstruction of data taken at multiple spatial points or with light of multiple spatial frequencies. However, to our knowledge, this work is the first to employ the Rytov algorithm for tomographic reconstruction of hyperspectral optical imaging data. A key feature of the algorithm is its speed, as each hemodynamic time course consists of many time points (72 in the present study). By performing the calculation in the spatial Fourier domain and directly solving for the concentrations of oxy- and deoxyhemoglobin, the algorithm takes \(<15\) s to compute 3-D images at each time point using the large (\(\sim 2.5 \times 10^6\) data points) hyperspectral data sets. The combination of hyperspectral data collection methods and DOT algorithms potentially enhances ISOI by providing new information for localization and quantification of hemodynamic signals. To compare our results with established approaches and utilize the power of broadband spectral content, we have also calculated hemodynamic signal changes using the modified Beer–Lambert law, where the widely varying photon path length was accounted for using Monte Carlo modeling.

## 2 Methods

### 2.1 Animal Preparation

Rats were prepared for imaging using our standard protocol that has been described previously. Briefly, five male Sprague-Dawley rats were anesthetized with an intraperitoneal injection of Nembutal (55 mg/kg b.w.). Rats were also given an intramuscular injection of atropine (0.05 mg/kg b.w.) into the hind leg, and a subcutaneous injection of 5% glucose (3 mL). Supplemental injections of Nembutal (27.5 mg/kg b.w.) were given as necessary (approximately 1/h). Body temperature was monitored by a rectal probe and maintained at 37°C using a self-regulating heating blanket. Skin and muscle were removed from the area over the left primary somatosensory cortex, and a 6 \( \times \) 8 mm imaging window was made by thinning the skull to a thickness of \( \sim 150 \) \( \mu \)m using a dental drill. Petroleum jelly was built around the thinned skull region, filled with saline, and capped with a glass coverslip, keeping the thinned skull moist and translucent during the imaging procedure. All performed procedures were in compliance with National Institutes of Health guidelines and approved by the University of California Animal Care and Use Committee.

### 2.2 Imaging Protocol

In each imaging trial, sensory stimulation consisted of five deflections at 5 Hz to the right C2 whisker. For each deflection, a copper wire displaced the whisker 0.8 mm along the rostral-caudal axis at a distance of 5 mm from the C2 follicle for a duration of 100 ms. Images were acquired with an exposure time of 50 ms at a rate of 5 Hz beginning 1.5 s before stimulus onset and lasting 15 s. For each rat, two blocks of 64 trials each were acquired with an intertrial interval of 15 s plus a random delay between 0 and 5 s. The imaging window was evenly illuminated by broadband light from a tungsten-halogen quartz lamp.

### 2.3 Hyperspectral Imaging

We have described our IMS system previously. Briefly, light remitted from the cortex is focused on a custom-made redirecting mirror composed of many long strips. Each strip has a slightly different 2-D tilt angle that reflects light in a different direction. A prism subsequently disperses the light from each strip before it arrives at a large-format CCD array. Each pixel on the CCD array corresponds to the light within a narrow wavelength band remitted from a point on the cortex. Therefore, images at the various wavelength bands are obtained by a simple mapping procedure, eliminating the need to reconstruct images.
Konecky et al.: Hyperspectral optical tomography of intrinsic signals in the rat cortex

as is done with other hyperspectral snapshot techniques such as computed tomography imaging spectrometry and coded aperture snapshot spectral imaging. For this paper, we acquired intrinsic signal images simultaneously at 38 separate wavelengths between 484 and 652 nm over a grid of 350 × 350 pixels using the image mapping spectrometer system. Our field of view was approximately 6 × 6 mm such that each pixel corresponded to a 17 × 17 μm area of the cortex. The width of each wavelength band Δλ(λ) varied continuously from Δλ = 3 nm at λ = 484 nm to Δλ = 8 nm at λ = 652 nm. A representative hyperspectral snapshot of a rat cortex acquired with a single 50-ms exposure appears in Fig. 1. The key advantage provided by the IMS is that it simultaneously acquires images at all 38 wavelengths, enabling brain imaging at multiple frames per second, a critical feature for resolving the rapid hemodynamic signatures of neurovascular coupling in response to stimulus.

2.4 Data Analysis

2.4.1 Intrinsic signal

For each block of 64 trials, we averaged the imaged reflectance at each time point over the 64 trials. For each time point, the averaged data set consisted of a data cube consisting of 38 × 350 × 350 pixel images, with each image corresponding to one wavelength bin. We averaged the three exposures immediately preceding stimulation onset to calculate the baseline intensity. The intrinsic signal for each time point was then calculated for each tissue-scattering coefficient of μs = 10 mm⁻¹, and tissue-scattering anisotropy of g = 0.9, similar to values we have measured previously in this animal model using quantitative spatial frequency domain imaging.

2.4.2 Modified Beer–Lambert law

In order to generate 2-D images of the changes in hemoglobin concentrations, we used the modified Beer–Lambert law, which appears as

\[ \phi(t) = -[\varepsilon_{\text{HBO}_2}(\lambda)\delta c\text{tHBO}_2(t) + \varepsilon_{\text{Hb}}(\lambda)\delta c\text{tHb}(t)]L(\lambda). \] (1)

Here, \( \varepsilon_{\text{HBO}_2} \) and \( \varepsilon_{\text{Hb}} \) are the extinction coefficients for oxy- and deoxyhemoglobin, \( \delta c\text{tHBO}_2(t) \) and \( \delta c\text{tHb}(t) \) are the changes in tissue concentration of those chromophores relative to their baseline values, and \( L(\lambda) \) is the mean photon path length in the cortex as a function of wavelength. Monte Carlo simulations were used to determine the mean path lengths traveled by photons of differing wavelengths. In our Monte Carlo simulations, we began by using tissue oxy- and deoxyhemoglobin concentrations of \( \text{ctHBO}_2 = 60 \mu\text{M} \) and \( \text{ctHb} = 40 \mu\text{M} \), respectively, tissue-scattering coefficient of \( \mu_s = 10 \text{ mm}^{-1} \), and tissue-scattering anisotropy of \( g = 0.9 \), similar to values we have measured previously in this animal model using quantitative spatial frequency domain imaging.

2.4.3 Rytov approximation

While the modified Beer–Lambert law has been used extensively to produce images of changes in hemoglobin concentration, Eq. (1) assumes that the changes occur uniformly throughout the brain. The Rytov approximation is a generalization of the modified Beer–Lambert law that allows one to solve for spatially varying changes in chromophore concentrations.

---

Fig. 1: Snapshot of the rat cortex at 38 wavelengths simultaneously with the image mapping spectrometer during a single 50-ms exposure. Light remitted from the cortex is imaged onto the mapping mirror, which is composed of many strips. Each strip reflects the light focused on it to a different location. The light from each strip is dispersed by a prism before reaching the CCD array. Each location on the CCD array corresponds to a wavelength of light and a point on the cortex. A simple mapping procedure reorganizes the data to produce the spectrally resolved images.
By taking advantage of the differing penetration depths of visible and near-infrared light in the cortex, we can implement the Rytov approximation to generate 3-D images of the changes in Hb and HbO₂ concentrations.

The propagation of multiple-scattered incoherent light in tissue is governed by the radiative transport equation (RTE)

\[ \mathbf{s} \cdot \nabla I(\mathbf{r}, \mathbf{s}) + \mu_t I(\mathbf{r}, \mathbf{s}) = \mu_a I(\mathbf{r}, \mathbf{s}) + \mathbf{S}(\mathbf{r}, \mathbf{s}), \]

where \( I(\mathbf{r}, \mathbf{s}) \) is the specific intensity, \( \mu_a \) and \( \mu_t \) are the absorption and scattering coefficients, respectively, \( \mu_a = \mu_a + \mu_s \) is the extinction coefficient, \( A(\mathbf{s}, \mathbf{s}') \) is the phase function, and \( S(\mathbf{r}, \mathbf{s}) \) describes the source. The RTE allows us to relate the changes in light intensity detected at location \( \mathbf{r}_d \) in direction \( \mathbf{s}_d \) to changes in the concentrations of Hb and HbO₂, by use of the Rytov approximation

\[ \phi(\lambda, \mathbf{r}_d, \mathbf{s}_d) = -\int d^3 r d^3 s I(\lambda, z, \mathbf{s}) G(\lambda, \mathbf{r}, \mathbf{s}, \mathbf{r}_d, \mathbf{s}_d) \delta \mu_a(\lambda, \mathbf{r}), \]

where

\[ \phi(\lambda, \mathbf{r}_d, \mathbf{s}_d) = I(\lambda, z = 0, \mathbf{s}) \log \frac{R(\lambda, \mathbf{r}_d, \mathbf{s}_d)}{R_0(\lambda, \mathbf{r}_d, \mathbf{s}_d)} \]

is the data function, \( I(\lambda, z, \mathbf{s}) \) is the specific intensity of the planar illumination in the cortex, \( G(\lambda, \mathbf{r}, \mathbf{s}, \mathbf{r}_d, \mathbf{n}) \) is the Green’s function for the RTE, and the change in absorption is decomposed into a sum of the contributions from changes in cHb and cHbO₂

\[ \delta \mu_a(\lambda, \mathbf{r}) = \epsilon_{\text{Hb}}(\lambda) \delta \text{cHb}(\mathbf{r}) + \epsilon_{\text{HbO₂}}(\lambda) \delta \text{cHbO₂}(\mathbf{r}). \]

We solve Eq. (4) using a correction to the standard diffusion approximation that accounts for the fact that near boundaries, the specific intensity is not isotropic. Using this correction, we can rewrite Eq. (4) as

\[ \phi(\lambda, \mathbf{r}_d) = \int d^3 r d^3 s I(\lambda, z) G(\lambda, \mathbf{r}, \mathbf{r}_d) - \frac{\ell^2}{3} \nabla I(\lambda, z) \cdot \nabla G(\lambda, \mathbf{r}, \mathbf{r}_d) c \delta \mu_a(\lambda, \mathbf{r}). \]

Here, \( I(\lambda, z) \) is the photon density, \( \ell^* = 1/(\mu_a + \mu_s) \) is the transport mean free path, \( c \) is the speed of light, \( \mathbf{r}_d \) is a 2-D vector specifying the detector location, and the Green’s function \( G(\lambda, \mathbf{r}, \mathbf{r}') \) satisfies the diffusion equation

\[ [D(\lambda) \nabla^2 + c \mu_a(\lambda)] G(\lambda, \mathbf{r}, \mathbf{r}') = \delta(\mathbf{r} - \mathbf{r}'), \]

with the diffusion coefficient \( D = c \ell^* \). In Eq. (6), we have assumed that the source and detected light are oriented normal to the tissue surface.

Equation (7) is the most easily inverted in the Fourier domain where it is block diagonal. Taking a 2-D Fourier transform with respect to the detector position \( \mathbf{r}_d \) yields a 1-D integral for each value of the Fourier coefficient \( \mathbf{q} \)

\[ \tilde{\phi}(\lambda, \mathbf{q}) = \int d z \kappa(\lambda, q, z) \tilde{\delta} \mu_a(\lambda, \mathbf{q}, z). \]

The function \( \kappa(\lambda, q, z) \) can be calculated from Eq. (7) using known expressions for the Green’s functions of the diffusion equation. In the semi-infinite geometry, we have

**Fig. 2** Absorber concentration [averaged over a region of interest (ROI) and normalized to peak] as a function of depth, calculated for simulated data using the Rytov-approximation-based optical tomography algorithm described in Sec. 2.4.2. The data functions were generated by using Monte Carlo software to simulate the two-dimensional surface reflectance at different wavelengths for a tissue model with a sub-surface absorbing inclusion (10x the absorption of the surroundings) buried beneath 0.5 mm of tissue and having an extent of 2 mm in the z-direction (as denoted by the blue box overlaid on the figure). The reconstructed center depth of the inclusion was defined as the z-value at which the reconstructed concentration had its highest value. The reconstructed extent of the inclusion was defined as the full-width at half-maximum of the curve describing the concentration as a function of depth. For this case, the multi-spectral tomography algorithm reconstructed the center depth and thickness of the inclusion to within 23% and 18%, respectively.
\[ \kappa(\lambda, q, z) = \left( \frac{\ell}{D} \right)^2 \left[ 1 - \frac{\ell^2}{3} Q(\lambda, q)Q(\lambda, 0) \right] \times \left( \frac{\exp \left[ (Q(\lambda, q) + Q(\lambda, 0))z \right]}{(Q(\lambda, q)\ell + 1)(Q(\lambda, 0)\ell + 1)} \right), \]  

(9)

where \( \ell \) is the extrapolation length, defined as the distance from the boundary at which the energy density reaches zero, and \( Q(\lambda, q) = (c_\mu a / D + q^2)^{1/2} \). The changes in ctHb and ctHbO2, relative to baseline, are then calculated according to

\[ \delta \text{ctHb}(\rho, z) = \frac{d^2 q}{(2\pi)^2} \exp(-i\rho \cdot \rho) \sum_{m,n} \epsilon_{\text{HB}}(\lambda_m) \kappa * (\lambda_m, q, z) M_{m,n}^{-1}(q) \tilde{\phi}(\lambda_m, q), \]  

(10)

\[ \delta \text{ctHbO}_2(\rho, z) = \frac{d^2 q}{(2\pi)^2} \exp(-i\rho \cdot \rho) \sum_{m,n} \epsilon_{\text{HbO}_2}(\lambda_m) \kappa * (\lambda_m, q, z) M_{m,n}^{-1}(q) \tilde{\phi}(\lambda_m, q). \]  

(11)

We compute the matrix elements of \( M(q) \) analytically according to

**Fig. 3** Imaging changes in light intensity. (a) Images of the cortex using 570 nm light are overlaid with color images representing the change in remitted light at 529 nm (isosbestic point sensitive to total hemoglobin concentration) and 630 nm (primarily sensitive to deoxyhemoglobin). Time points correspond to the initial decrease in signal at 630 nm, the decrease at 529 nm, and the overshoot at 630 nm. The purple/yellow color scale indicates an increase in remitted light, while the green/blue scale represents a decrease. (b) Time course of remitted light intensity for the ROI (see Sec. 2) at an isosbestic point (529 nm), deoxyhemoglobin peak (557 nm), oxyhemoglobin peak (576 nm), and at 630 nm. (c) Spectra of the intrinsic signal during the time points pictured in (a). (d) False color representation of intrinsic signal as a function of both time and wavelength. (e) Spectra of oxy- and deoxyhemoglobin. (b, c) Error bars represent the standard error over all pixels in the ROI. Regions of interest were determined by selecting a pixel in the 630 nm image where a maximum drop in measured light intensity occurred, and then averaging over a 500 mm x 500 mm area surrounding that pixel.
eq.12

\[
M_{m,n}(q) = \int_0^\infty dz [\varepsilon_{\text{Hb}}(\lambda_m)\varepsilon_{\text{Hb}}(\lambda_n) + \varepsilon_{\text{HbO}_2}(\lambda_m)\varepsilon_{\text{HbO}_2}(\lambda_n)] \kappa(\lambda_m, q, z) + \kappa(\lambda_n, q, z) \]

and then find its inverse by solving its eigenvalue problem. The inversion is regularized by setting eigenvalues below a threshold to zero.

The framework of this Rytov-approximation-based algorithm has previously been shown to provide accurate estimates of depth of buried fluorescent inclusions in small animals. In addition, we have recently performed a validation of the hyperspectral tomography algorithm on data generated using Monte Carlo simulations with a 2-mm thick absorbing inclusion buried 0.5 mm beneath the surface. For this case (Fig. 2), the multispectral tomography algorithm was able to accurately reconstruct the center depth of the inclusion to within 23% and the inclusion thickness to within 18%. A more detailed discussion of tomography validation studies, employing both tissue-simulating phantoms and computational models of the forward problem, will be the subject of a future report (currently in preparation).

3 Results and Discussion

Figure 3 demonstrates our ability to image the changes in light intensity due to functional activation with high spatial and temporal resolution simultaneously at many wavelengths through a thinned skull in a representative rat. Figure 3(a) shows images of changes in light remitted from the cortex at 529 nm (isosbestic point equally sensitive to oxy- and deoxyhemoglobin) and 630 nm (about 9x more sensitive to deoxyhemoglobin than oxyhemoglobin).

Color maps of the change in light intensity are superimposed over black and white images at 576 nm, which clearly show the underlying vasculature. As can be seen by looking at the time dependence of the signal over the area of peak activation shown in Fig. 3(b), the time points chosen in Fig. 1(a) correspond to the initial decrease in the 630 nm signal, the time at which the isosbestic wavelength (529 nm) has its largest signal, and the increase of signal at 630 nm. Complete spectral information for these three time points is shown in Fig. 3(c), and the intrinsic signal is represented in Fig. 3(d) in false color as a function of both wavelength and time. These results are in agreement with our previous ISOI imaging at a single wavelength.

Representative images of the changes in ctHb and ctHbO2 along with traces of the region of interest calculated using the modified Beer–Lambert law appear in Figs. 4(a) and 4(b).

Fig. 4 Representative images of changes in concentration and with varied wavelengths. (a) Images of the change in tissue concentration of deoxy- and oxyhemoglobin for a representative rat at time points corresponding to the initial ctHb increase (1.1 s), the ctHbO2 increase (3.1 s), and the ctHb decrease (3.7 s), obtained using the modified Beer–Lambert law. Color maps of the hemoglobin changes are overlaid above an image of the cortex at 570 nm. The purple/yellow color scale indicates an increase in concentration, while the green/blue scale represents a decrease. (b, c) Time-resolved changes in ctHb and ctHbO2 for the ROI on the cortex, obtained using the modified Beer–Lambert law, for (b) all wavelengths and (c) only for the wavelengths 529 and 630 nm. Error bars represent the standard error for all pixels in the ROI.
Changes in concentration (Table 1, averaged over all rats) were determined using the modified Beer–Lambert law, where optical path lengths were determined using Monte Carlo simulations of photon transport. The peak increase in ctHbO2 (6ctHbO2 = 248 ± 80 nM) was ~3× greater than the ctHb decrease (6ctHb = −84 ± 20 nM). The peak changes in concentration did not occur at the same time; the peak change in total hemoglobin arose first (tHbT = 2.6 ± 0.4 s), followed by the peak in ctHbO2 (tHbO2 = 3.1 ± 0.3 s), and the maximum decrease in ctHb (tHb = 4.3 ± 0.3 s).

We varied the number of wavelengths used to fit for ctHb and ctHbO2 to determine the effect on the recovered changes in hemoglobin concentration. We found that using fewer wavelengths led to additional noise in the recovered hemoglobin values. For example, Figs. 4(b) and 4(c) shows the hemoglobin time courses for a single rat using all 38 wavelengths [Fig. 4(b)], and only using two wavelengths [Fig. 4(c)]: an isosbetic wavelength (529 nm) and a deoxyhemoglobin sensitive wavelength (630 nm). When reducing the number of wavelengths from 38 to 2, the standard error of hemoglobin concentration changes in the regions of interest increased from 6 to 20 nM for ctHbO2 and from 3.5 to 5.6 nM for ctHb. However, despite the increase in noise, removing wavelengths did not significantly alter the timing or peak magnitudes of the hemodynamic time courses.

We also conducted Monte Carlo simulations over a wide range of parameters to determine the effect of path length on the calculated values for changes in ctHb and ctHbO2. Figure 5 illustrates the variability in the magnitude of hemoglobin changes calculated when different baseline optical properties are assumed. The variability of the initial ctHb increase, the ctHbO2 increase, and the subsequent ctHb decrease are reported in Table 2. Increasing the baseline value of total hemoglobin or scattering leads to an increase in the magnitude of all parameters. This occurs because an increase in absorption or scattering decreases the mean photon path length. Since the data remain fixed, this leads to an increase in the calculated hemoglobin concentrations (see Sec. 2). All changes due to varying the wavelength dependence of scattering, described by $A_{\lambda}^{b}$ where the $A$ and $b$ parameters refer to scattering amplitude and power, respectively, were less than 15% despite changing scattering power, $b$, over a large range ($b = 0$–2.5).

Future work will include a quantitative comparison between the tomography model used in this paper and a Monte Carlo-based tomography model that uses photon path length information stored in the simulations to provide accurate quantification of absorber depth and concentration. Future work will also include a detailed computational investigation into the influence of tissue background absorption and scattering properties on the depth sensitivity of the optical tomography algorithm. This future study will also include a systematic investigation into how the background optical properties and the set of wavelengths employed affect the ability of the algorithm to fully separate oxygenated hemoglobin absorption from deoxygenated hemoglobin absorption. This future work will include a quantitative comparison between the tomography model used in this paper and a Monte Carlo-based tomography model that uses photon path length information stored in the simulations to provide accurate quantification of absorber depth and concentration.

Figure 6 shows representative depth-resolved snapshots of the changes in oxy- and deoxyhemoglobin at 4 s poststimulus for one rat. These images were calculated according to the Rytov approximation method described in Sec. 2.4.2. Eleven wavelengths from 586 to 652 nm were employed in the reconstructions. Slices of the 3-D images of ctHb and ctHbO2 are shown at six depths from 100 μm to 1.1 mm beneath the surface of the cortex. Depth profiles of the changes in oxy- and deoxyhemoglobin, as a function of depth beneath the surface of the cortex, are shown in Fig. 7(a) for the same rat as in Fig. 6. Figure 7(b) shows time courses of these changes in oxy- and deoxyhemoglobin, at a depth of 0.3 mm beneath the surface of the cortex, averaged over four rats.

The time courses shown in Fig. 7(b) illustrate an initial decrease in the concentration of oxygenated hemoglobin and an initial increase in the concentration of deoxygenated hemoglobin over the first 2 s poststimulus, followed by an increase in the oxyhemoglobin concentration and a decrease in the deoxyhemoglobin concentration over the subsequent 5 s. Using the Rytov tomography algorithm, the maximum changes in ctHbO2 and ctHb were found to occur at depths of 0.29 ± 0.02 and 0.66 ± 0.04 mm beneath the surface of the cortex, respectively. The peak

<table>
<thead>
<tr>
<th>Parameter varied in Monte Carlo simulation</th>
</tr>
</thead>
<tbody>
<tr>
<td>HbT (ctHbO2 + ctHb)</td>
</tr>
<tr>
<td>---------------------</td>
</tr>
<tr>
<td>50 μM</td>
</tr>
<tr>
<td>ctHbO2 increase (nM)</td>
</tr>
<tr>
<td>ctHb decrease (nM)</td>
</tr>
</tbody>
</table>

Table 2: Magnitude of changes in hemoglobin concentrations for the differing optical properties used in the Monte Carlo simulations.
Fig. 5 Time courses for the concentrations of oxy- and deoxyhemoglobin, averaged over all rats, where the optical properties have been varied when determining the mean photon path length used in the modified Beer-Lambert law. The values of (a) total tissue hemoglobin concentration (HbT), (b) tissue hemoglobin oxygenation (StO$_2$), (c) scattering coefficient ($\mu_s$), and (d) scattering power ($b$ parameter, see text) were varied. Error bars indicate the standard error for all rats.

Fig. 6 Representative three-dimensional reconstructed images of changes in oxy- and deoxyhemoglobin for one rat in response to stimulus, obtained at time $t = 4$ s poststimulus using the Rytov approximation. Each panel represents a cross section at a given depth beneath the surface of the cortex. The concentration maps have been overlaid on 571-nm reflectance images of a 4.35 mm $\times$ 4.35 mm region of the cortex.
times and magnitudes of concentration changes for the 3-D image reconstructions are summarized in Table 1. For the Rytov tomography algorithm, the point of peak concentration change (Table 1) was defined as the peak time point at the depth \( z = 0.3 \text{ mm} \) beneath the surface of the cortex at which the peak change in oxyhemoglobin concentration occurred. The magnitudes of the peak changes in oxy- and deoxyhemoglobin concentration shown in Table 1 are larger for the Rytov tomography algorithm than the Beer–Lambert method; this finding is expected because the Rytov tomography algorithm localizes the changes in 3-D space.

The results shown in Figs. 6 and 7 are indicative of the depletion of oxygen by the cortex in response to the stimulus, followed by the reperfusion of oxygenated blood into the region. Figures 6 and 7 also suggest that the relative magnitudes of the changes in oxy- and deoxyhemoglobin may vary with depth. This effect could possibly be explained by differences in depth of diving arterioles and venules, with the extraction of oxygen occurring deeper in the cortex and the reperfusion of oxygenated blood occurring closer to the surface. However, this effect may also represent a limitation of the ability of the Rytov tomography algorithm to localize the changes in deoxyhemoglobin concentration as precisely as the changes in oxyhemoglobin concentration (Figs. 6 and 7). This discrepancy could be due in part to the fact that the absorption features of oxy- and deoxyhemoglobin were not completely decoupled from each other due to the size of the wavelength bands detected by the image mapping spectrometer. Future studies will quantitatively examine this issue by convolving the oxy- and deoxyhemoglobin absorption spectra with the bandwidth profile \( \Delta \lambda (\lambda) \) of the detector.

4 Conclusion

We have employed a parallel hyperspectral imaging technique, IMS, to record intrinsic optical signals in the rat somatosensory cortex over 38 wavelength bands (from 484 to 652 nm) at 5 Hz following mechanical movement of a single whisker. This
The Rytov approach revealed that the maximum measured changes in ctHbO2 and ctHb were greater using the Rytov approximation than those estimated using the modified Beer–Lambert approach. One contribution to these differences in signal magnitude likely comes from the inability of planar reflectance methods to account for partial volume effects. The additional discrepancy between the ctHb values calculated with the Rytov and Beer–Lambert approaches is likely an artifact of the inability of the algorithm to completely separate the signal contributions from oxy- and deoxygenated hemoglobin. This is due, in part, to the fact that we did not rigorously characterize the effect of the wavelength dependence of detector bandwidth $\Delta\lambda(\lambda)$. Future studies will investigate potential improvements to the Rytov model as well as imposing further optical path length constraints through the use of structured light projection patterns.  

**Acknowledgments**

Support for this work was provided by the NIH Laser Microbeam and Medical Program (LAMMP, P41-EB015890), NIH R21 NS078634, R21 EB014440, R21 EB009186, and R01CA124319, and NINDS NS 666001 and NS 055832. We acknowledge the use of Virtual Photonics software resources (http://virtualphotonic.org/) supported by LAMMP. Soren D. Konecky was supported by a postdoctoral fellowship from the Hewitt Foundation for Medical Research. Robert H. Wilson is also supported by a postdoctoral fellowship from the Hewitt Foundation for Medical Research. Beckman Laser Institute programmatic support from the Beckman Foundation is also acknowledged.

**References**


Biographies for the authors are not available.