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# Optimization of a thermally tuned silicon-based reconfigurable optical power splitter with thermal isolations

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**Abstract.** In this paper, a thermally tuned silicon-based three-channel reconfigurable multimode interference (MMI) optical power splitter with four optimized thermal isolations is proposed. Specific and flexible reconfigurable functions ( $1 \times 1$ ,  $1 \times 2$ , and  $1 \times 3$  MMI splitters) can be achieved by thermally tuning the heaters. By using a beam propagation method, the optimum geometry of the heaters, desired refractive index changes, and phase shifts of the MMI splitter are calculated at first. The temperature distributions of the devices without and with the thermal isolations are then analyzed by using the finite element method. Thermal crosstalk between adjacent heaters is observed and the influence of the thermal isolation geometry on the thermal crosstalk is examined subsequently. The geometry of the thermal isolations is optimized based on the trade-off between the thermal tuning efficiency and optical output characteristics. Finally, satisfactory improvements with the proposed structure are demonstrated with high-thermal efficiency (the maximum power dissipation decreases reach 43.7% and 55.2% for  $1 \times 1$  and  $1 \times 2$  MMI splitters, respectively) and good optical output quality (the maximum excess losses are as low as 0.365, 0.388, and 0.272 dB for  $1 \times 1$ ,  $1 \times 2$ , and  $1 \times 3$  MMI splitters, respectively; the crosstalk is less than  $-21.27$  and  $-15.54$  dB for  $1 \times 1$  and  $1 \times 2$  MMI splitters, respectively). © The Authors. Published by SPIE under a Creative Commons Attribution 3.0 Unported License. Distribution or reproduction of this work in whole or in part requires full attribution of the original publication, including its DOI. [DOI: [10.1117/1.OE.56.1.017106](https://doi.org/10.1117/1.OE.56.1.017106)]

Keywords: reconfigurable multimode interference power splitter; thermo-optic effect; thermal isolation; finite element method; beam propagation method.

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## 1 Introduction

In recent years, silicon photonics has been paid great attention for a growing number of applications (e.g., optical communication, manufacturing, biotechnology, energy, etc.) due to its tremendous versatility.<sup>1</sup> The silicon photonics is commonly regarded as a promising solution for next-generation optical networks in terms of the low cost, high-refractive index contrast, and compatibility with mature complementary metal-oxide-semiconductor technologies.<sup>2</sup>

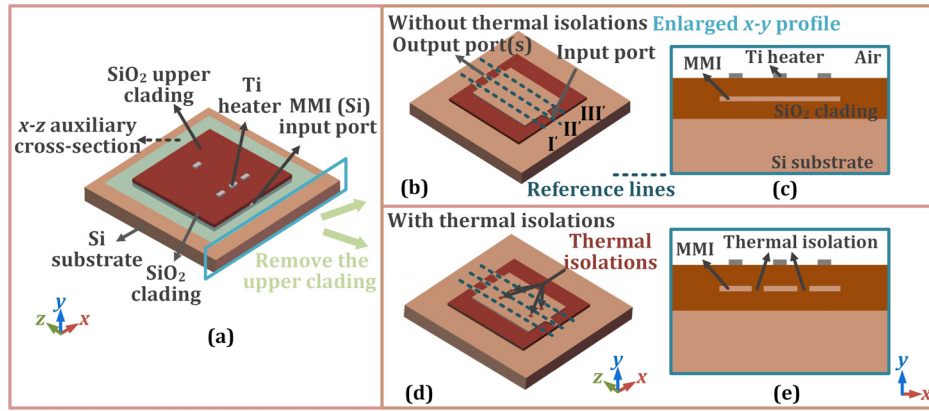
The optical power splitter is a key component for splitting light in optical communication networks.<sup>3,4</sup> In a silicon photonic circuit, power splitters are based on typical structures such as a microring,<sup>5</sup> directional coupler,<sup>6</sup> Y-branch,<sup>7</sup> and multimode interference (MMI) coupler.<sup>8</sup> Compared with the other structures, the MMI-based optical power splitter has the advantages of low excess losses (ELs) and crosstalk,<sup>9</sup> a wide optical bandwidth,<sup>10</sup> a compact size,<sup>11</sup> and large fabrication tolerances.<sup>12</sup> Thus, it is the ideal structure to realize the power splitting function. On the other hand, the reconfigurable functions are highly desired for the next-generation optical communication networks.<sup>13</sup> Fortunately, the optical power splitters can sufficiently offer us reconfigurable functionality and introduce further flexibility. The MMI-based optical power splitter is very suitable for achieving the reconfigurable function,<sup>14,15</sup> which may derivate novel integrated and compact photonics.<sup>16</sup>

By designing the MMI structure and modulating the refractive index of specific multimode (self-images) areas, the phase shifts in the MMI coupler can be accurately controlled,<sup>17–19</sup> and different splitting ratios at the output ports can then be realized.

There are generally two mechanisms to modulate the phase shifts in silicon photonics: current-injection tuning<sup>18</sup> and thermal tuning.<sup>20</sup> The current-injection tuning scheme is a great option that satisfies the need for a high-tuning speed.<sup>21</sup> However, this scheme uses a complex excess doping process, which makes the fabrication more complex.<sup>22</sup> Moreover, a doping process with different types and dopant concentrations will introduce more ELs. Therefore, the thermal tuning scheme is preferred to achieve the desired phase shifts on the client side without the need for a high-tuning speed. To improve the thermal tuning efficiency, investigators have still been making continuous efforts to work on developing advanced methods such as using optimized heaters<sup>23</sup> and waveguides with optimized thermal isolation structures.<sup>24</sup>

In this paper, a thermally tuned silicon-based three-channel reconfigurable MMI optical power splitter with four optimized thermal isolations is proposed. To fulfill specific reconfigurable functions ( $1 \times 1$ ,  $1 \times 2$ , and  $1 \times 3$  MMI splitters), the optimum geometry of the heaters, desired refractive index changes, and phase shifts of the MMI splitter are designed at first by using the beam propagation method (BPM). Next, the temperature distributions of the devices with and without the thermal isolations are calculated by using the finite element method (FEM) with the appropriate heating powers. By varying the geometry of the thermal

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**Fig. 1** (a) Geometric schematic of the thermally tuned MMI coupler. (b) Geometric schematic of the MMI without thermal isolations with the silica upper cladding removed and (d) with four thermal isolations. (c, e) Cross-sections of the MMI corresponding to (b) and (d).

isolations, thermal crosstalk between adjacent heaters is observed; meanwhile, the influence of thermal isolation geometry on the thermal crosstalk is examined. Finally, the geometry of the thermal isolations is optimized to ensure high-thermal efficiency (i.e., low-power dissipation) and good optical outputs (e.g., low losses and crosstalk, good uniformity, etc.).

## 2 Device Structure and Basic Mechanisms

The proposed thermally tuned reconfigurable optical power splitter is composed of one multimode waveguide connected to one input port and three output ports, as shown in Fig. 1. The waveguide structure (ridge waveguide) can be fabricated by electron beam lithography (EBL) and inductively coupled plasma (ICP) etching. A silica upper cladding layer (can be deposited on the silicon waveguide structure) and lower cladding layer are fashioned to the MMI coupler, as shown in Fig. 1(a). This structure is located on a silicon substrate. Figures 1(b) and 1(c) show the device's internal structure without the thermal isolations for clearer visualization, while Figs. 1(d) and 1(e) give similar drawings of the device with thermal isolations consisting of material with low-thermal conductivity (i.e., silica in this study) to increase the thermal tuning efficiency. Since the etching depth of the trenches is the same as the thickness of the MMI, we can realize these thermal isolations by etching some trenches on the MMI structure, until to the oxide layer (SiO<sub>2</sub>), at the same time with the fabrication process of the MMI waveguide structure by EBL and ICP etching. In these figures, the reference lines I', II', and III' are marked to help in the analysis of the temperature distributions of specific thermal tuning areas. These

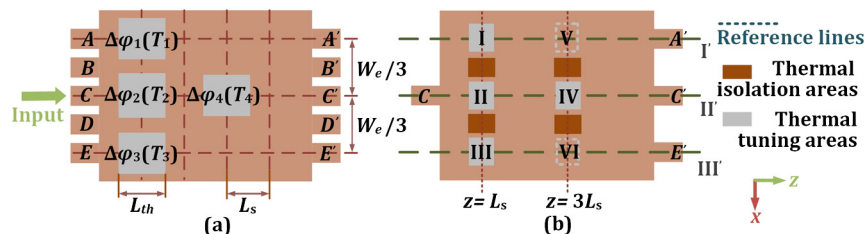
lines go across the MMI couplers along the  $z$ -axis direction and are just beneath the heaters.

Figure 2(b) describes the prototype of the  $1 \times 3$  MMI coupler, which is based on a  $5 \times 5$  MMI: without affecting the functions, the input waveguides  $A, B, D$ , and  $E$  and the output waveguides  $B'$  and  $D'$  are removed to reduce the crosstalk between each channel. Four titanium heaters are designed at specific positions (marked I–IV):  $0.7 \mu\text{m}$  above the silica upper cladding. Then the refractive index of the Si multimode waveguide beneath the heaters can be modulated by the thermo-optic effect. We achieve desired phase shifts to fulfill certain functions by heating these specific thermal tuning functions (I–III is at  $z = L_s$  and IV is at  $z = 3L_s$ ), as shown in Fig. 2(b). Based on the self-imaging theory,<sup>17</sup> the effective width  $W_e$  and beating length  $L_\pi$  of the two lowest-order modes can be defined as

$$W_e \approx W_{\text{MMI}} + \left(\frac{\lambda_0}{\pi}\right) \left(\frac{n_c}{n_r}\right)^{2\sigma} (n_r^2 - n_c^2)^{-1/2}, \quad (1)$$

$$L_\pi = \frac{\pi}{\beta_0 - \beta_1} \approx \frac{4n_r W_e^2}{3\lambda_0}, \quad (2)$$

where  $W_{\text{MMI}}$  is the width of multimode waveguide,  $W_e$  is the effective width considering the lateral penetration depth of each mode field ( $\sigma = 0$  for transverse electric (TE) modes and  $\sigma = 1$  for transverse magnetic modes),  $\lambda_0$  is the input wavelength (set to 1550 nm in this study),  $n_r$  and  $n_c$  are the effective refractive indices of the multimode waveguide (silicon) and lateral cladding material (silica), respectively, and  $\beta_0$  and  $\beta_1$  are the propagation constants of the zeroth



**Fig. 2** (a) Schematic diagram of a thermally tuned  $5 \times 5$  MMI coupler. (b) Layout of the device in our study: the thermal tuning areas and thermal isolation positions are marked.

and first lateral modes, respectively. For simplicity, we consider only the situation for TE modes; thus,  $W_e \approx W_{\text{MMI}}$ .

The general matrix theory of self-imaging in MMI couplers with single-mode input and output waveguides is used,<sup>18,25</sup> and the multimode waveguide is split into five subsections with the same length  $L_s$ , as shown in Fig. 2(a). This is the shortest length for a theoretically lossless  $5 \times 5$  MMI coupler:

$$L_s = \left( \frac{1}{N+1} \cdot \frac{2n_r W_e^2}{\lambda_0} \right) |_{N=5} = \left( \frac{1}{N+1} \cdot \frac{3L_\pi}{2} \right) |_{N=5} = \frac{L_\pi}{4}, \quad (3)$$

thus, the length of the MMI coupler  $L_{\text{MMI}} = 5/4 L_\pi$ . In the multimode waveguide of the MMI coupler, if the phase shifts caused by the thermo-optic effect are taken, the complex image amplitudes in the output guides  $E_{\text{out}}$  from the complex object amplitudes in the input guides  $E_{\text{in}}$  can be described as

$$\begin{aligned} [E_{A'}, E_{B'}, E_{C'}, E_{D'}, E_{E'}]_{\text{out}}^T &= M_s \cdot M_s \cdot T_{3P} \cdot M_s \cdot M_s \cdot T_{1P} \\ &\cdot M_s \cdot [E_A, E_B, E_C, E_D, E_E]_{\text{in}}^T, \end{aligned} \quad (4)$$

where  $M_s$  is the transfer matrix of complex image amplitudes in each subsection with  $L_s$ , and the diagonal matrices  $T_{3P}$  and  $T_{1P}$  can describe the phase shifts at those specific thermal tuning positions (I–IV). The corresponding equations are as follows:

$$\begin{aligned} T_{3P} &= \text{diag}(e^{-j\varphi_I}, 1, e^{-j\varphi_{II}}, 1, e^{-j\varphi_{III}}) \\ T_{1P} &= \text{diag}(1, 1, e^{-j\varphi_{IV}}, 1, 1), \end{aligned} \quad (5)$$

where  $\varphi_i$  ( $i = \text{I} - \text{IV}$ ) are the shifted phases of corresponding I–IV thermal tuning areas.

In the proposed reconfigurable three-channel optical power splitter, the output power in each port is thermally tunable, providing three reconfigurable functions:  $1 \times 1$ ,  $1 \times 2$ , and  $1 \times 3$  optical power splitter. To achieve these functions, the desired phase shifts of the I–IV thermal tuning areas are easily calculated based on Eqs. (4) and (5):

$$\begin{aligned} (\varphi_I, \varphi_{II}, \varphi_{III}, \varphi_{IV})_{1 \times 1 \text{ MMI}} &= (2/3\pi, 2/3\pi, 0, 0), \\ (\varphi_I, \varphi_{II}, \varphi_{III}, \varphi_{IV})_{1 \times 2 \text{ MMI}} &= (0, 5/12\pi, 1/4\pi, 0), \\ (\varphi_I, \varphi_{II}, \varphi_{III}, \varphi_{IV})_{1 \times 3 \text{ MMI}} &= (0, 0, 0, 0). \end{aligned} \quad (6)$$

Then the thermally induced refractive index change can be introduced to achieve these phase shifts:

$$\Delta\varphi = k \cdot \Delta n \cdot L_t, \quad (7)$$

$$\Delta n = \frac{\partial n}{\partial T} \cdot \Delta T, \quad (8)$$

where  $\Delta\varphi$  is the phase shift caused by thermal tuning,  $k$  is the wavelength number,  $\Delta n$  is the thermally induced refractive index change, and  $L_t$  is the length of the thermal tuning section.  $L_t$  is approximate to the length of the Ti heater  $L_h$ .  $\partial n / \partial T$  is the refractive index derivative with regard to the temperature (unit:  $\text{K}^{-1}$ ), and  $\Delta T$  is the temperature difference

between the triple self-images located in the thermal tuning areas (I–III or IV–VI) with the same  $z$ -coordinates ( $z = L_s$  or  $z = 3L_s$ ).

To obtain the temperature distribution, the following thermal conduction equation needs to be solved:

$$\frac{\partial T(x, y, z, t)}{\partial t} - \frac{K}{\rho C} \nabla^2 T(x, y, z, t) = \frac{Q(x, y, z, t)}{\rho C}, \quad (9)$$

where  $(x, y, z)$  is the space coordinates,  $T$  is the temperature,  $t$  is the time, and  $Q(x, y, z, t)$  is the heat generation rate defined as the heat generation power for a unit volume. The static form of the thermal conduction equation is

$$K \nabla^2 T(x, y, z) + \frac{P_i}{V_i} = 0 \quad (i = \text{I} - \text{IV}), \quad (10)$$

where  $P_i$  ( $i = \text{I} - \text{IV}$ ) is the heating power and  $V_i$  is the volume of each heater.

In this study, material properties such as the density  $\rho$  (unit:  $\text{kg} \cdot \text{m}^{-3}$ ), specific heat  $C$  (unit:  $\text{J} \cdot \text{kg}^{-1} \cdot \text{K}^{-1}$ ), and thermal conductivity  $K$  ( $\text{W} \cdot \text{m}^{-1} \cdot \text{K}^{-1}$ ) are regarded as temperature-independent and are listed in Table 1. The initial geometric parameters of the device are listed in Table 2.

### 3 Simulation and Optimization

Four thermal isolations in specific positions are designed in the thermally tuned reconfigurable MMI power splitter to boost the thermal tuning efficiency. Meanwhile, to ensure good outputs, some parameters are needed to be optimized such as the heater geometry, heating powers, and thermal isolation geometry. For these complex analyses, taking the thermo-optic effects into account, the temperature distributions and the optical output characteristics of the proposed structure are simulated and analyzed then.

**Table 1** Material properties used in the simulation ( $\lambda_0 = 1550$  nm,  $T = T_{\text{ambient}} = 300$  K).

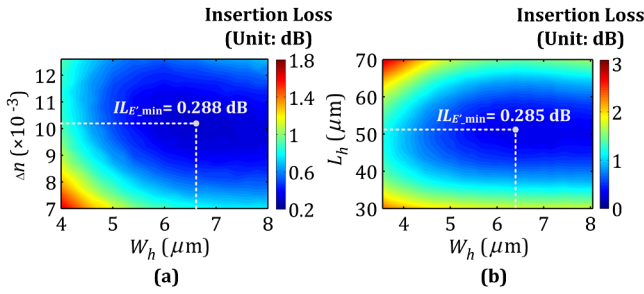
Material	$n$	$\partial n / \partial T$	$\rho$	$C$	$K$	References
Si	3.475	$1.84 \times 10^{-4}$	2329	714	148	[MLC], 26
SiO <sub>2</sub>	1.445	$1.0 \times 10^{-5}$	2203	730	1.4	[MLC], 27

Note: [MLC] refers to the Material Library in the COMSOL Multiphysics software.

**Table 2** Initial geometric parameters of the device for simulation (unit:  $\mu\text{m}$ ).

$W_{\text{MMI}}$	$L_{\text{MMI}}$	$H_{\text{MMI}}$	$W_{\text{taper}}$	$L_{\text{taper}}$	$W_{\text{wg}}$
32	3848	0.22	5	56	3
$W_c$	$L_c$	$H_c$	$L_{\text{sub}}$	$H_{\text{sub}}$	$H_h$
128	3848	8	4000	100	0.1

Note:  $W$ ,  $L$ , and  $H$  represent the width, length, and height (or thickness) of each component. The subscript  $\text{wg}$  refers to the single-mode waveguide,  $c$  refers to the silica cladding,  $\text{sub}$  refers to the silicon substrate, and  $h$  refers to the heater.



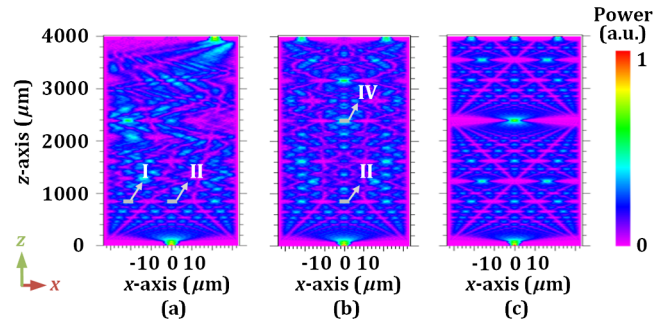
**Fig. 3** (a) IL of the output port  $E'$  ( $IL_{E'}$ ) depending on  $W_h$  when  $\Delta n_s$  is changed ( $L_h = 50 \mu\text{m}$ ). (b) Contour diagram  $L_h$ - $W_h$  with  $IL_{E'}$  when  $\Delta n_I = \Delta n_{II}$  is  $10.2 \times 10^{-3}$  (in the case of  $1 \times 1$  MMI power splitter).

We initially set the length of the heater  $L_h$  to  $50 \mu\text{m}$ , similar to Rosa et al.<sup>20</sup> Naturally, for a  $1 \times 1$  MMI power splitter, temperature rises of the thermal tuning areas (I and II) in the MMI  $\Delta T_I = \Delta T_{II} = 56.2 \text{ K}$  are needed to get corresponding refractive index change  $\Delta n_I = \Delta n_{II} = 1.033 \times 10^{-2}$ , which leads to a  $2\pi/3$  phase shift. For the  $1 \times 2$  MMI power splitter,  $\Delta T_{II} = 35.1$  and  $\Delta T_{IV} = 21.1 \text{ K}$  are needed to get  $\Delta n_{II} = 6.458 \times 10^{-3}$  and  $\Delta n_{IV} = 3.875 \times 10^{-3}$ , which leads to  $5\pi/12$  and  $\pi/4$  phase shifts at thermal tuning areas II and IV, respectively.

However, the geometry of the heater will affect the output characteristics of the MMI coupler, especially for the insertion loss (IL) and the excess loss (EL). To choose the appropriate geometric parameters of the heater, we first considered the situation for the  $1 \times 1$  MMI power splitter: the width of the heater  $W_h = 6.6 \mu\text{m}$  is chosen to obtain the minimum IL of the output port  $E'$  with the value  $0.288 \text{ dB}$ , while  $\Delta n_I = \Delta n_{II} = 10.2 \times 10^{-3}$  as depicted in Fig. 3(a). Based on the contour diagram of  $L_h$ - $W_h$  in Fig. 2(b), if  $\Delta n_I = \Delta n_{II}$  is set to the optimum value of  $10.2 \times 10^{-3}$ ,  $L_h$  and  $W_h$  can then be optimized to  $51$  and  $6.4 \mu\text{m}$ , respectively. In this case, the EL can be as low as  $0.248 \text{ dB}$ , and the crosstalk of the output ports ( $A' - E'$  and  $C' - E'$ ) can be less than  $-25.94 \text{ dB}$  (not the minimum but acceptable).

By using the same method for the  $1 \times 2$  MMI power splitter,  $L_h$  and  $W_h$  can be optimized to  $51$  and  $6.4 \mu\text{m}$ , respectively, while  $\Delta n_{II} = 6.34 \times 10^{-3}$  and  $\Delta n_{IV} = 3.8 \times 10^{-3}$ . The EL would be as low as  $0.324 \text{ dB}$ , the crosstalk of  $C' - A'$  and  $C' - E'$  would be less than  $-15.72 \text{ dB}$ , and the uniformity of the output ports  $A'$  and  $E'$  would be better than  $2.9 \times 10^{-3} \text{ dB}$ . For the  $1 \times 3$  MMI power splitter, the heater geometry would have a much smaller influence on the output characteristics of the MMI coupler than in the other two cases because there is no thermally induced phase shift. When  $L_h$  and  $W_h$  are set to  $51$  and  $6.4 \mu\text{m}$ , respectively, the EL is as low as  $0.144 \text{ dB}$ , and the uniformity of the output ports  $A'$ ,  $C'$ , and  $E'$  is better than  $1.2 \times 10^{-3} \text{ dB}$ . Considering all these factors, the geometric parameters of the heater are finally optimized to  $L_h = 51 \mu\text{m}$  and  $W_h = 6.4 \mu\text{m}$ .

As known the desired phase shifts and thermally induced refractive index changes in these different cases, we can then determine the desired heating powers of the heaters and corresponding temperature rises in the specific thermal tuning areas by sweeping the heating powers with a power step of  $0.1 \text{ mW}$ . For the  $1 \times 1$  MMI power splitter, when the heating powers of heaters I and II are  $P_I = 16.2 \text{ mW}$  and  $P_{II} = 21.5 \text{ mW}$ , the temperature difference between the specific areas (II and III on the reference lines II' and III' with



**Fig. 4** Optical power distributions of the silicon-based three-channel optical power splitter at  $1550 \text{ nm}$ : (a)  $1 \times 1$ , (b)  $1 \times 2$ , and (c)  $1 \times 3$  MMI power splitters.

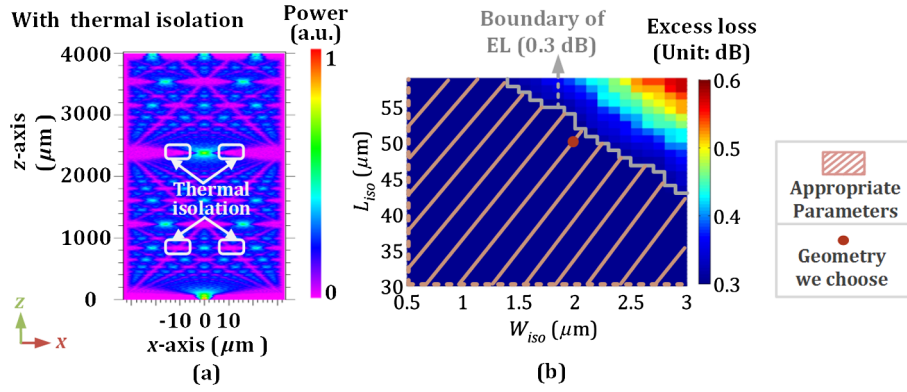
$z = L_s$ ) reaches  $\Delta T_{\text{max}} = 55.2 \text{ K}$ , and the accumulated phase shift is about  $0.668\pi$ . For the  $1 \times 2$  MMI power splitter, when the heating powers of heaters II and IV are, respectively,  $P_{II} = 20.9 \text{ mW}$  and  $P_{IV} = 13.4 \text{ mW}$ , the temperature differences between the specific areas (I and II on the reference lines I' and II' with  $z = L_s$  and V and IV on the reference lines I' and II' with  $z = 3L_s$ ) reach  $\Delta T_{\text{max}} = 34.5$  and  $20.7 \text{ K}$ , respectively, and the accumulated phase shifts are about  $0.418\pi$  and  $0.251\pi$ , accordingly.

By incorporating the above thermally induced refractive index changes and phase shifts into our simulation, we finally obtain the optical power distributions of the silicon-based three-channel optical power splitter at  $1550 \text{ nm}$ , as shown in Fig. 4.

Next, thermal isolations are further added to the designs of the three MMI power splitters discussed above. Detailed thermal simulations are performed by using FEM to analyze the temperature distributions and thermally induced phase shifts. The thermal effects are considered to finally calculate the outputs of the devices based on BPM. Compared with the MMI power splitters without thermal isolations, the optimized device has much higher thermal efficiency and much lower heating power consumption. It should be noted, however, that the influences of the thermal isolation geometry on the device outputs should not be ignored. There is a trade-off between the thermal tuning efficiency and optical outputs.

First, the positions of the thermal isolations are needed to be optimized, in order to minimize the impact on the device outputs in terms of excess loss, which is found to be located where the optical field is weak enough. Thus, the best positions are located just in the middle of the adjacent thermal tuning areas with the same  $z$ -coordinate ( $z = L_s$  or  $z = 3L_s$ ), as shown in Fig. 2(b). Figure 5(a) shows the optical power distribution of the  $1 \times 3$  MMI power splitter with thermal isolations ( $L_{iso} = 50 \mu\text{m}$ ,  $W_{iso} = 2 \mu\text{m}$ ) at an input wavelength of  $1550 \text{ nm}$ . This figure clearly shows the thermal isolations. Similar to the case without thermal isolations, the desired refractive index changes are incorporated into our simulation, and the EL is then examined when the geometry of the thermal isolation is varied ( $L_{iso}$ :  $30$  to  $60 \mu\text{m}$ ,  $W_{iso}$ :  $0.5$  to  $3 \mu\text{m}$ ). It is clear that a smaller isolation area would benefit a smaller EL of the splitter. However, to compromise the trade-off between the thermal tuning efficiency and the optical outputs, we need to choose the optimum geometry parameters of the thermal isolation area.

We assume that the EL of less than  $0.3 \text{ dB}$  is acceptable, as shown in Fig. 5(b). We then draw a reference line



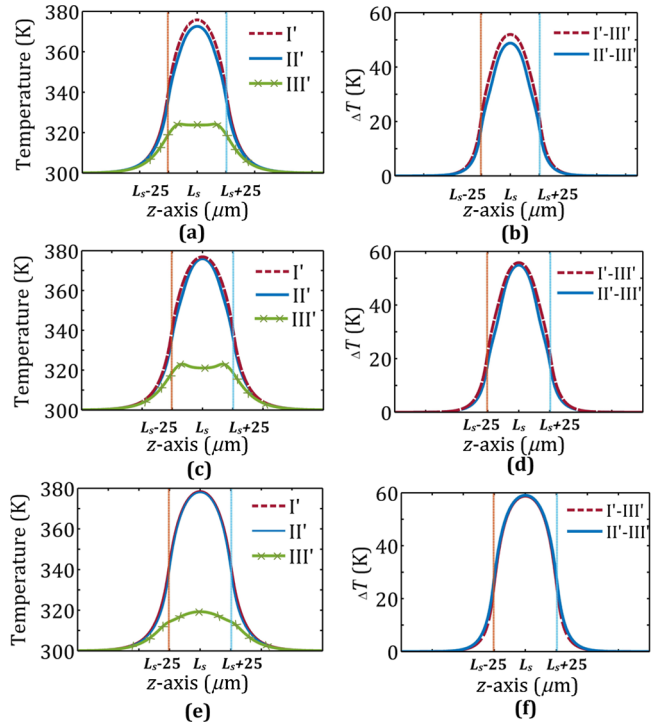
**Fig. 5** (a) Optical power distribution of the  $1 \times 3$  MMI power splitter with thermal isolations at 1550 nm. (b) ELs of the power splitter when the geometry of the thermal isolation changes for  $1 \times 3$  MMI power splitters.

(boundary line) to facilitate our observation. The shadow triangle with a reference indicates the region for appropriate parameters, and the red point is corresponding to the geometry parameters we choose. Similarly, for the  $1 \times 1$  and  $1 \times 2$  MMI power splitters (these two cases are with thermal effects), the EL is also calculated in detail for different geometric parameters of the thermal isolations ( $L_{iso}$ : 35 to 65  $\mu\text{m}$ ,  $W_{iso}$ : 0.5 to 2.5  $\mu\text{m}$ ). For the cases  $1 \times 1$  and  $1 \times 2$  MMI power splitters, we assume that EL of less than 0.4 dB is acceptable in these two cases.

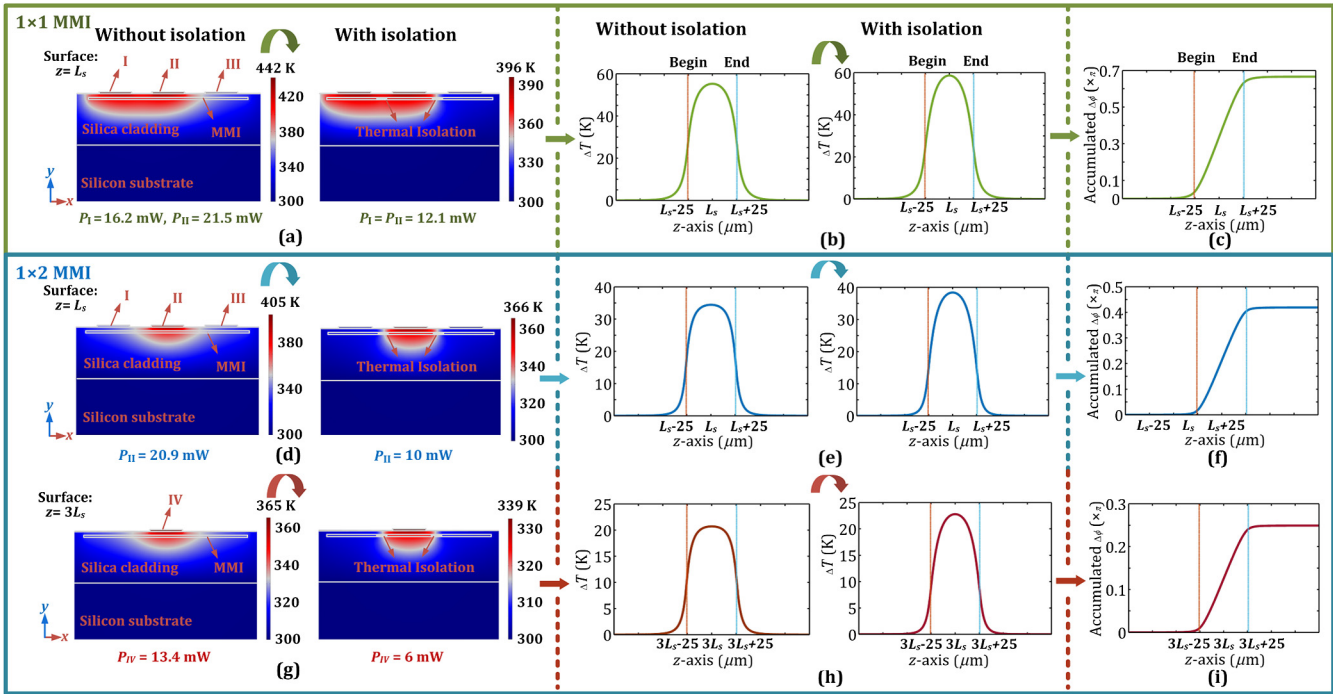
To optimize the geometry of the thermal isolations, the appropriate region is further examined. For the  $1 \times 1$  MMI power splitter, the heating powers of heaters I and II ( $P_I$  and  $P_{II}$ ) are both set to 12 mW, and three design geometries of the isolations are studied:  $(L_{iso}, W_{iso}) = (30 \mu\text{m}, 1 \mu\text{m})$ ,  $(30 \mu\text{m}, 2 \mu\text{m})$ , and  $(50 \mu\text{m}, 2 \mu\text{m})$ . Figure 6 shows the one-dimensional temperature distributions of the reference lines [corresponding to lines I'–III' in Fig. 2(b)] and the temperature differences between these lines. Based on the temperature distributions in Figs. 6(a), 6(c), and 6(e), the temperatures of lines I' and II' increase and become close to equal when the size of the isolation is increased. Meanwhile, the temperatures of line III' decrease obviously. The trend of the temperature changes shows that the influence of thermal crosstalk gradually decreases when the size of the isolation is increased. In more detail, based on the changes in the temperature differences described in Figs. 6(b), 6(d), and 6(f), the heat from the heater clearly seems to be “blocked” by the thermal isolations. Figure 6(f) shows that the temperature differences of (I'–III') and (II'–III') are clearly much closer (even equal) compared with those in Fig. 6(b). Therefore, we infer that the thermal crosstalk between each adjacent heater can be eliminated if the geometry of the thermal isolation is large enough, and we set  $L_{iso} = 50 \mu\text{m}$  and  $W_{iso} = 2 \mu\text{m}$  as our final geometric parameters of the isolations. The fabrication tolerance of our device is concerned in practice, and estimated value is about 0.1  $\mu\text{m}$  (the EL changes are within  $\pm 0.6\%$ ).

Improvements on thermal tuning efficiency with the thermal isolations are demonstrated with the simulated results in Fig. 7. Figures 7(a), 7(d), and 7(g) show the two-dimensional temperature distributions on cross-sectional drawings ( $x - y$  axis) of the  $1 \times 1$  and  $1 \times 2$  MMIs without and with the silica trench. In the optimized device, the heating power of the heaters is as follows. For the  $1 \times 1$  MMI,  $P_I = P_{II} =$

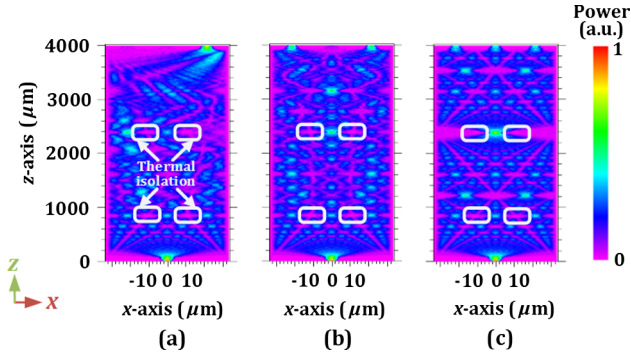
12.1 mW (compared with those used in MMI without thermal isolations, the power dissipations are reduced by 25.3% and 43.7%, respectively). For the  $1 \times 2$  MMI,  $P_{II} = 10 \text{ mW}$  and  $P_{IV} = 6 \text{ mW}$  (compared with those used in the MMI without thermal isolations, the power dissipations are reduced by 52.2% and 55.2%, respectively). Figures 7(b), 7(e), and 7(h) present the temperature differences. For the  $1 \times 1$  MMI, the maximum temperature difference  $\Delta T_{\text{max}}$  reaches 58.7 K. For the  $1 \times 2$  MMI,  $\Delta T_{\text{max}}$  reaches 38.3 K (heating by heater II) and 22.8 K (heating by heater IV), respectively. The final accumulated phase shifts are then obtained as shown in Figs. 7(c), 7(f), and 7(i):  $0.666\pi$ ,  $0.419\pi$ , and  $0.249\pi$  for the  $1 \times 1$ ,  $1 \times 2$ , and  $1 \times 3$  MMI power splitters, respectively.



**Fig. 6** For the  $1 \times 1$  MMI power splitter, one-dimensional temperature distributions of the reference lines [corresponding to lines I'–III' in Fig. 2(b)] and the temperature differences between these lines if  $P_I = P_{II} = 12 \text{ mW}$ : (a, b)  $L_{iso} = 30 \mu\text{m}$ ,  $W_{iso} = 1 \mu\text{m}$ ; (c, d)  $L_{iso} = 30 \mu\text{m}$ ,  $W_{iso} = 2 \mu\text{m}$ ; and (e, f)  $L_{iso} = 50 \mu\text{m}$ ,  $W_{iso} = 2 \mu\text{m}$ .



**Fig. 7** (a, d, g) Two-dimensional temperature distributions along the cross-section ( $x - y$  axis) of the  $1 \times 1$  and  $1 \times 2$  MMIs without and with silica trenches. (b, e, h) Maximum temperature difference  $\Delta T_{\max}$  for  $1 \times 1$  and  $1 \times 2$  MMIs, respectively. (c, f, i) Final accumulated phase shifts for the  $1 \times 1$  and  $1 \times 2$  MMIs, respectively.



**Fig. 8** Optical power distributions of the optimized MMI power splitters at 1550 nm: (a)  $1 \times 1$ , (b)  $1 \times 2$ , and (c)  $1 \times 3$  MMIs.

However, it should be noticed that the desired temperature rises of the MMI power splitter with thermal isolations are slightly greater than those without thermal isolations because the isolations reduce the temperature difference more markedly at the edges of the heater [see Figs. 7(b), 7(e), and 7(h)]. Thus, the effective tuning areas [below the curves and above the  $z$ -axis, as shown in Figs. 7(b), 7(e), and 7(h)] of the MMI power splitter with thermal isolations will be slightly smaller if the desired temperature rises are set to the same value.

Finally, we obtained the optical power distributions of the optimized  $1 \times 1$ ,  $1 \times 2$ , and  $1 \times 3$  MMI power splitters at 1550 nm, as shown in Fig. 8. For the  $1 \times 1$  MMI power splitter, the EL is as low as 0.365 dB and the crosstalk of  $A' - E'$  and  $C' - E'$  is less than  $-21.27$  dB. For the  $1 \times 2$  MMI power splitter, the EL is as low as 0.388 dB and the crosstalk of  $C' - A'$  and  $C' - E'$  is less than  $-15.54$  dB. The uniformity of the output ports  $A'$  and  $E'$  is better than

**Table 3** Results of the outputs without and with thermal isolations.

Reconfigurable functions	EL (dB)	Crosstalk (dB)	Uniformity (dB)	Heating powers (mW)	Total powers (mW)
$1 \times 1$ MMI <sub>without</sub>	0.248	$-25.94$	—	$P_I = 16.2, P_{II} = 21.5$	37.7
$1 \times 1$ MMI <sub>with</sub>	0.365	$-21.27$	—	$P_I = P_{II} = 12.1$	24.2
$1 \times 2$ MMI <sub>without</sub>	0.324	$-15.72$	$2.9 \times 10^{-3}$	$P_{II} = 20.9, P_{IV} = 13.4$	34.3
$1 \times 2$ MMI <sub>with</sub>	0.388	$-15.54$	$3.1 \times 10^{-3}$	$P_{II} = 10, P_{IV} = 6$	16
$1 \times 3$ MMI <sub>without</sub>	0.144	—	$1.2 \times 10^{-3}$	—	—
$1 \times 3$ MMI <sub>with</sub>	0.272	—	$1.9 \times 10^{-3}$	—	—

$3.1 \times 10^{-3}$  dB. For the  $1 \times 3$  MMI power splitter, the EL is as low as 0.272 dB and the uniformity of the output ports  $A'$ ,  $C'$ , and  $E'$  is better than  $1.9 \times 10^{-3}$  dB. Table 3 compares the final outputs with regard to the cases without and with thermal isolations. It clearly shows the improvements with our design.

#### 4 Conclusion

In this paper, we have proposed a thermally tuned silicon-based three-channel reconfigurable MMI optical power splitter with four optimized thermal isolations. The specific and flexible reconfigurable functions ( $1 \times 1$ ,  $1 \times 2$ , and  $1 \times 3$  MMI splitters) are achieved by thermally tuning the heaters. By using BPM, the optimum geometry of the heaters, the desired refractive index changes, and phase shifts of the MMI splitter are calculated at first. Next, the temperature distributions of the devices without and with the thermal isolations are analyzed by using FEM. Thermal crosstalk between adjacent heaters is observed by comparing the temperature changes with regard to different geometries of the thermal isolations. We find that the thermal crosstalk between adjacent heaters can clearly be eliminated if the thermal isolation has sufficiently large geometry. To compromise the trade-off between the thermal tuning efficiency and optical output quality, the geometry of the thermal isolation is optimized to  $L_{iso} = 50 \mu\text{m}$  and  $W_{iso} = 2 \mu\text{m}$ . With the optimum parameters, a high-thermal efficiency (the maximum power dissipations for the  $1 \times 1$  and  $1 \times 2$  MMI splitters are reduced by 43.7% and 55.2%, respectively) and good optical output characteristics (the maximum EL values are as low as 0.365, 0.388, and 0.272 dB for the  $1 \times 1$ ,  $1 \times 2$ , and  $1 \times 3$  MMI splitters, respectively; the crosstalk is less than  $-21.27$  and  $-15.54$  dB for the  $1 \times 1$  and  $1 \times 2$  MMI splitters, respectively) have been demonstrated.

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